# Georg-August-Universität Göttingen Module B.Mat.3121: Introduction to algebraic geometry

### 9 C 6 WLH

# Learning outcome, core skills:

#### Learning outcome:

In the modules of the cycle "Algebraic geometry" students get to know the most important classes of algebraic varieties and schemes as well as the tools for studying these objects and the mappings between them. The students apply these skills to problems of arithmetic or complex analysis. They are introduced to current research questions and enabled to carry out independent contributions to research, e. g. within the scope of a Master's thesis.

Algebraic geometry uses and connects concepts of algebra and geometry and can be used versatilely. In the course offer several aspects are considered at a time and a cycle will only cover some of the learning objectives mentioned below. The introduction to the cycle and the specialisation in the cycle will normally cover different aspects of algebraic geometry and supplement one another complementarily. The following content-related competencies are pursued. Students

- are familiar with commutative algebra, also in greater detail;
- know the concepts of algebraic geometry, especially varieties, schemes, sheafs, bundles;
- examine important examples like elliptic curves, Abelian varieties or algebraic groups;
- · use divisors for classification questions;
- · study algebraic curves;
- prove the Riemann-Roch theorem and apply it;
- use cohomological concepts and know the basics of Hodge theory;
- apply methods of algebraic geometry to arithmetical questions and obtain e. g. finiteness principles for rational points;
- classify singularities and know the significant aspects of the dimension theory of commutative algebra and algebraic geometry;
- get to know connections to complex analysis and to complex geometry.

#### Core skills:

After having successfully completed the module, students will be able to

- discuss basic concepts of the area "Algebraic geometry";
- explain basic ideas of proof in the area "Algebraic geometry";
- illustrate typical applications in the area "Algebraic geometry".

# Workload: Attendance time: 84 h Self-study time: 186 h

Course: B.Mat.3121.Lec Lecture course (Lecture)	4 WLH
Examination: Written or oral examwritten examination (120 minutes) or oral	9 C
examination (appr. 20 minutes)	
B.Mat.3121.Mp: Introduction to algebraic geometry	
Examination prerequisites:	

B.Mat.3121.Ue: Achievement of at least 50% of the exercise points and presentation, twice, of solutions in the exercise sessions	
Course: B.Mat.3121.Ex Exercise session (Exercise)	2 WLH
Examination requirements:  Proof of knowledge and mastery of basic competencies in the area "Algebraic geometry"	

Admission requirements:	Recommended previous knowledge: B.Mat.1100, B.Mat.1200
Language: English	Person responsible for module: Dean of studies
Course frequency: not specified	Duration: 1 semester[s]
Number of repeat examinations permitted: twice	Recommended semester: Bachelor: 5 - 6; Master: 1 - 4
Maximum number of students: not limited	

## Additional notes and regulations:

Instructor: Lecturers at the Mathematical Institute